

Ex from Meeting 2 of LSE PH 500

$H_0: \mu \leq 150$ vs. $H_1: \mu > 150$ (Let $\sigma = 10$, $n = 25$)

let significance level $\alpha = .025$

Reject iff $M > 150 + 2SE$ (N-P)

Reject H_0 whenever $M \geq 150 + 2\sigma/\sqrt{n}$: $M \geq 154$

M is the sample mean, its value is M_0 .

$$1SE = \sigma/\sqrt{25} = 10/5 = 2$$

Reject H_0 whenever $M \geq 150 + 2(2)$: $M \geq 154$

Let $M_0 = 154$, just at the .025 cut-off.

Assess SEV for the same claims in Table 3.1 p. 144

Claim $\mu > 149$

SEV ($\mu > 149$) = $\Pr(M \leq 154; 149)$

$Z = (154 - 149)/2 = 2.5$

$\Pr(Z \leq 2.5) = .99$

Now consider

Claim $\mu > 150$ (for the same outcome $M = 154$)

$$\text{SEV}(\mu > 150) = \Pr(M \leq 154; 150)$$

$$Z = (154 - 150)/2 = 2$$

$$\Pr(Z \leq 2) = .97$$

Now consider

Claim $\mu > 151$ (for the same outcome $M = 154$)

$$\text{SEV}(\mu > 151) = \Pr(M \leq 154; 151)$$

$$Z = (154 - 151)/2 = 1.5$$

$$\Pr(Z \leq 1.5) = .93$$

Now consider

Claim $\mu > 152$ (for the same outcome $M = 154$)

$$\text{SEV}(\mu > 152) = \Pr(M \leq 154; 152)$$

$$Z = (154 - 152)/2 = 1$$

$$\Pr(Z \leq 1) = .84$$

Now consider

Claim $\mu > 153$ (for the same outcome $M = 154$)

$$\text{SEV}(\mu > 153) = \Pr(M \leq 154; 153)$$

$$Z = (154 - 153)/2 = .5$$

$$\Pr(Z \leq .5) = .69$$

Add one beyond that table

Claim $\mu > 154$ (for the same outcome $M = 154$)

$$\text{SEV}(\mu > 154) = \Pr(M \leq 154; 154)$$

$$Z = (154 - 154)/2 = 0$$

$$\Pr(Z \leq 0) = .5$$

The warrant gets worse and worse for larger discrepancies given the same outcome